

# Analysing Meta-Model Product Lines

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# Motivation

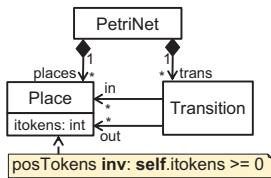
## Meta-model variants

- Meta-models are used to define modelling languages
- Different variants of a modelling language depending on scenario, project, goal...
- Having a meta-model for each variant is challenging to construct, analyse and maintain

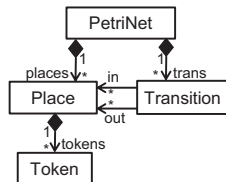
# Motivation

Example: variants of Petri nets

Different  
realizations



tokens as attributes

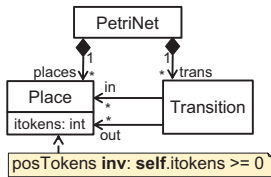


tokens as objects

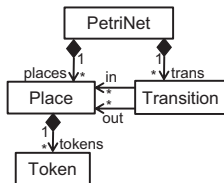
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Different realizations

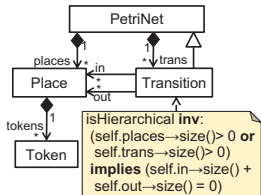


tokens as attributes

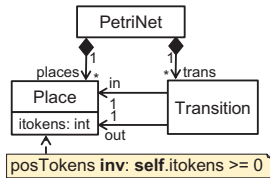


tokens as objects

Different features



hierarchical nets

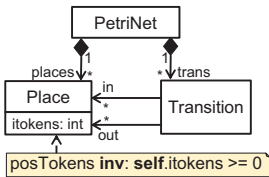


state-machine nets

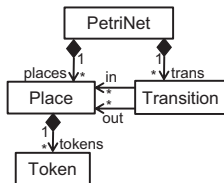
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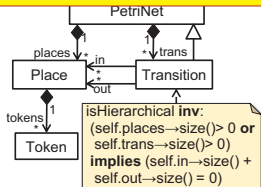
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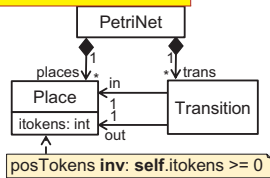
tokens as objects

8 possible meta-models

Different features



hierarchical nets



state-machine nets

# Motivation

Meta-model product lines (MMPLs)

## **Meta-model product line:**

compact representation of all meta-model variants

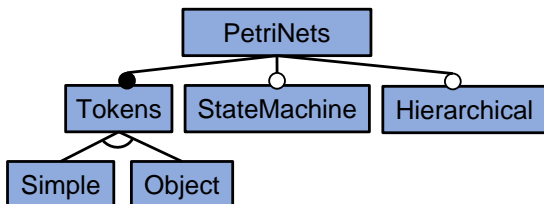
# Motivation

Meta-model product lines (MMPLs)

## Meta-model product line:

compact representation of all meta-model variants

### Feature Model



Valid feature configurations:

- Simple xor Object
- StateMachine is optional
- Hierarchical is optional

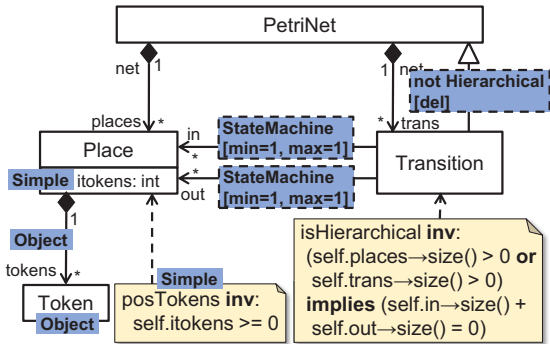
# Motivation

## Meta-model product lines (MMPLs)

### Meta-model product line:

compact representation of all meta-model variants

#### 150-Meta-Model



- Presence conditions
- Cardinality modifiers
  - min
  - max
- Inheritance modifiers
  - add
  - del



# Motivation

Meta-model product lines (MMPLs)

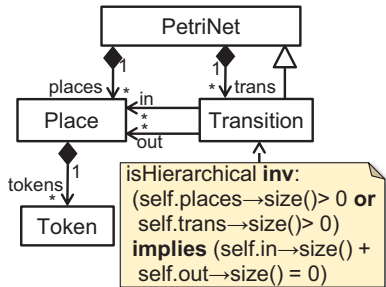
## Meta-model product line:

compact representation of all meta-model variants

### Feature Configuration

<Object, Hierarchical>

### Meta-Model Derivation



# Motivation

## Correctness of MMPLs

How to ensure a MMPL is correct?

- 1 ensure each meta-model is syntactically correct  
e.g., the target class of each meta-model reference belongs to the meta-model
- 2 ensure desirable properties in meta-model instances  
e.g., instantiability

There are well-known techniques to analyse this for a single meta-model.

However, generating and analysing each meta-model in the MMPL separately is time-consuming...

# Contribution

- We lift meta-model analysis techniques to the product line level:
  - syntactic analysis of meta-models
  - satisfiability checking of meta-model propertiesin order to improve performance
- Based on a declarative notion of MMPL
  - considers OCL well-formedness constraints
  - amenable to automated analysis
- Tool support
- Evaluation of effectiveness of lifted analyses

# Ensuring Well-formedness of Meta-Model Product Lines

# Ensuring MMPL well-formedness

## Lifted analysis of well-formed structure

- Every field is owned by one class  
How: PC of field  $\implies$  PC of its owner-class
- Every reference points to a class  
How: PC of reference  $\implies$  PC of its target-class
- Cardinality and inheritance are uniquely determined  
How: PC of  $\min_i \wedge$  PC of  $\min_j$  is unsat (similar for max, inheritance)
- There are no inheritance cycles  
How (roughly): given a cycle in the 150MM, the conjunction of the PC of each inheritance relation is unsat

# Ensuring MMPL well-formedness

## Lifted syntactic analysis of invariants

- If an invariant is present, the accessed elements are also present  
How: PC of invariant  $\implies$  PC of accessed fields + owner classes

Example:

PC of self.itokens  $\geq 0 \implies$  PC of itokens and PC of Place

Simple  $\implies$  Simple  $\wedge$  true

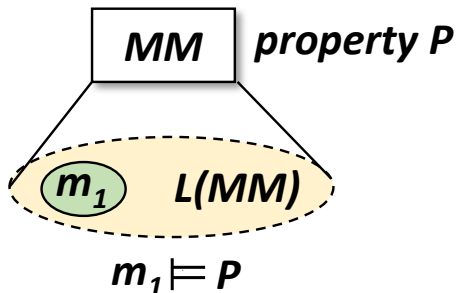
- Operators are applied on fields with appropriate cardinality  
How: if a collection operator is applied on a field, the PC of invariant  $\wedge$  PC of any max=1 is unsat

# Analysing Properties of Meta-Model Instances

# Analysing instance properties

## Meta-model validation by model finding

Is the set of models accepted by a meta-model the one intended?



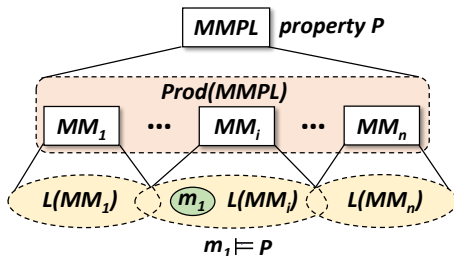
In the simplest case, if  $P$  is empty, this method permits assessing whether a meta-model has instances.



# Analysing instance properties

## MMPL validation

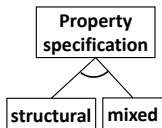
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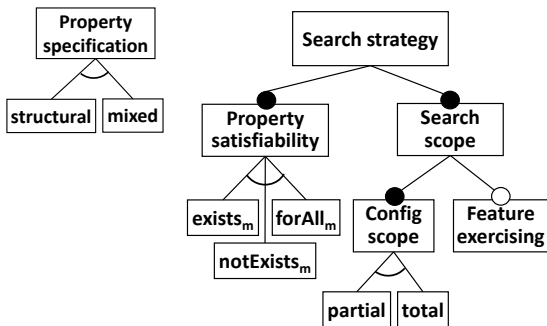
# Analysing instance properties

## Classification of property types



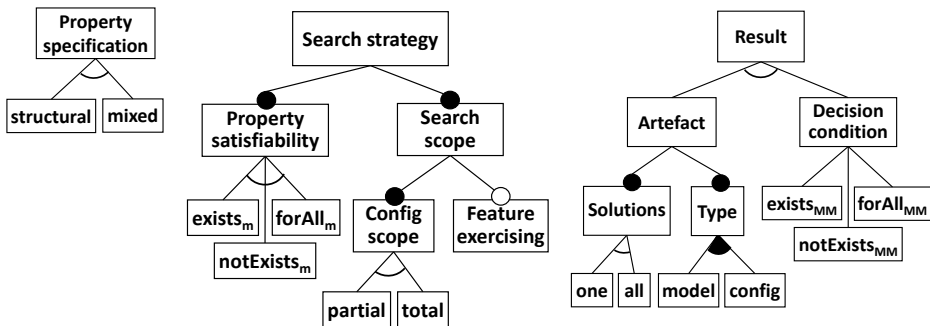
# Analysing instance properties

## Classification of property types



# Analysing instance properties

## Classification of property types



# Analysing instance properties

## Property types

Some analyses of interest (8 more in the paper):

- MMPL instantiability: configuration that yields an instantiable MM  
Configuration:  $\langle one, config, total, exists_m \rangle$
- Global invariant: is a property satisfied by every model of every MM?  
Example: all Petri nets have at least one place  
Configuration:  $\langle forAll_{MM}, forAll_m, \dots \rangle$   
Property:  $Place.all() \rightarrow notEmpty()$
- Safety property: is a property satisfied by no model?  
Example: no model has isolated transitions  
Configuration:  $\langle forAll_{MM}, notExists_m, \dots \rangle$   
Property:  $Transition.all() \rightarrow exists(in \rightarrow isEmpty() \text{ and } out \rightarrow isEmpty())$

# Analysing instance properties

## Property types

We also consider mixed properties

Example: Are transitions with one input only possible on state machines?

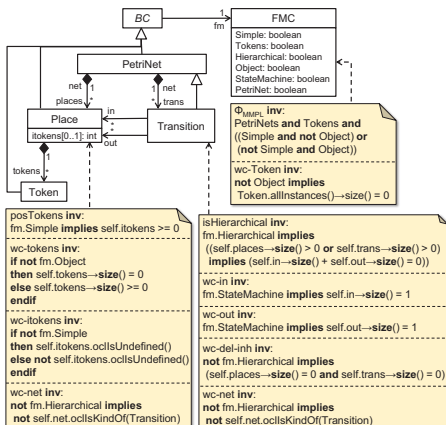
Configuration:  $\langle mixed, \dots \rangle$

Property:  $Transition.all() \rightarrow \text{forAll}(in \rightarrow size() = 1) \text{ implies } StateMachine$

# Lifted analysis of meta-model instances

## (1) Encoding of MMPL as a regular meta-model

### Feature-explicit meta-model



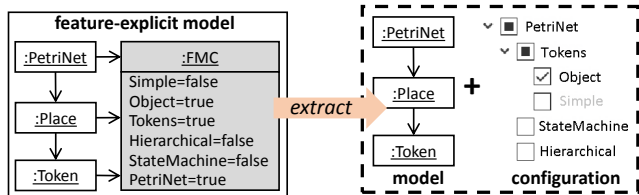
- 150MM
- Feature model is class FMC, where features are booleans
- PCs and modifiers are invariants
- Property to check is invariant

# Lifted analysis of meta-model instances

## (2) Analysing feature-explicit meta-model

Look for an instance of the FEMM using a model finder

- MMPL instantiability, weak properties (MMs where some model satisfies P): finding a solution implies satisfaction



- Safety properties (MMs where no model satisfies P): find all configs where some model satisfies P, and then return the rest
- Global invariants (MMs where all models satisfy P): find all configs where some model satisfies **not** P, and then return the rest



# Tooling

- Eclipse plugin: <http://miso.es/tools/merlin>
- Feature model specified with FeatureIDE
- 150MM specified as an Ecore meta-model with annotations
- Static analysis of OCL uses Eclipse OCL project and Sat4J
- USE Validator model finder

The screenshot displays the Eclipse IDE interface. On the left, the Project Explorer shows a project named 'PetriNets' containing files like 'model.xml' and 'PetriNets.ecore'. The main editor shows the content of 'PetriNets.ecore' with the following code:

```

property output : Place[*]
{
  annotation modifier
  (
    condition = 'StateMachine',
    min = '1',
    max = '1'
  );
  invariant isHierarchical:
  (places->size()>0 or trans->size()>0)
  implies
  (input->size()=0 and output->size()=0)
}

```

On the right, the 'PetriNets Model' diagram shows a hierarchy: 'PetriNet' is the root, branching into 'StateMachine' and 'Hierarchical'. 'Hierarchical' further branches into 'Tokens', which then branches into 'Simple' and 'Object'.

In the foreground, the 'Model property analysis' dialog is open. It displays the property: 'Transition.allInstances()->forAll(t | t.input->size()=1) implies \$StateMachine'. The dialog includes search options for property satisfaction (set to 'all models'), feature exercising (unchecked), and partial configuration (empty). The result section shows 'Produce witness models' and 'Produce configurations' checked, and 'Number of solutions' set to 'all'. 'OK' and 'Cancel' buttons are at the bottom.

Merlin

# Evaluation

# Evaluation

## Efficiency of syntactic analysis

### Enumerative approach vs Lifted analysis

Name	#Feats	#MMs	#classes/#invs /#PCs/#modifs	Lifted time	Enum time
Running example	6	8	4/2/5/2	<b>0,039s</b>	0,19s
Relational DDBB	10	24	7/0/17/0	<b>0,094s</b>	0,45s
Graphs [29]	16	256	5/6/14/3	<b>0,103s</b>	22,36s
Automata	20	2.016	6/5/18/0	<b>0,135s</b>	102,9s
Role modelling [27]	48	>2.395.000	40/0/32/9	<b>0,735s</b>	>1h

⇒ Lifted analysis was much faster

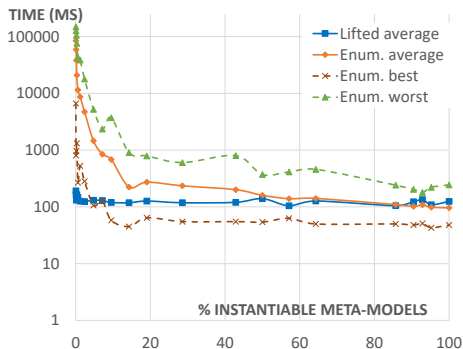
# Evaluation

## Efficiency of instance property analysis

- Enumerative approach vs Lifted analysis
- MMPL instantiability (finding an instantiable meta-model)
  - Enumerative approach:
    - 1 generate product meta-model
    - 2 check meta-model instantiability by model finding
    - 3 if the meta-model has instances, conclude
    - 4 else, go to 1
- 22 variants of the Automata MMPL, each with a different percentage of instantiable meta-models

# Evaluation

## Efficiency of instance property analysis



- Lifted analysis is (up to 1.000x) faster if  $<85\%$  instantiable MMs
- In the rest of cases, lifted analysis is slightly slower (120 vs 100 ms)

Rationale: 1 more complex search (lift.) *vs* many simpler searches (enum.)

⇒ **The fewer MMs satisfy a property, the faster lifted analysis is**

# Conclusions and Future Work

- MMPLS: Declarative specification of meta-model variants
- Lifting of existing meta-model analysis techniques to the PL level
  - syntactic correctness of meta-models
  - checking properties on meta-model instances
- Initial implementation and evaluation



## Current and next steps

- Transformation product lines, coupled to MMPLs

*Model transformation product lines. Juan de Lara, Esther Guerra, Marsha Chechik, Rick Salay. Proc. of ACM/IEEE MoDELS'18. pp. 67-77. ACM.*

- Extend definition of MMPL with type modifiers for references
- Expand analyses, e.g., to discover subsumption of MM variants
- Extend the evaluation for other kinds of properties

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## Questions?